## EG3111 Finite Element Analysis and Design

## **Exercise sheet #4: Beam and Frame Elements**

## Questions

1. Use two beam elements to solve the problem of a beam of length 2L fixed at both ends subject to a vertical load P N at the centre, as shown in Figure 1.



Figure 1: A beam subject to a central point load *P*.

2. Use two beam elements to solve the problem of a beam of length 2L fixed at both ends subject to a distributed load  $p_0$  N/m, as shown in Figure 2.



Figure 2: A beam subject to a uniformly distributed load  $p_0$ .

3. Use two beam elements to solve the problem of a beam of length 2L fixed at both ends subject to a linearly distributed load p(x) N/m, as shown in Figure 3.



Figure 3: A beam subject to a linearly distributed load p(x).

4. A framework formed from two frame elements, shown in Figure 4, is subjected to a horizontal point force *P*. The extensional stiffness of the elements is k = EA/L and the bending stiffness is  $\alpha = EI/L^3$ . Formulate the matrices required to find the unknown displacements, forces and moments. <u>Note</u>: there is no need to solve the 3x3 matrices.



Figure 4: A framework formed from two frame elements