## EG3111 Finite Element Analysis and Design

## Exercise sheet \#4: Beam and Frame Elements

## Questions

1. Use two beam elements to solve the problem of a beam of length $2 L$ fixed at both ends subject to a vertical load $P \mathrm{~N}$ at the centre, as shown in Figure 1.


Figure 1: A beam subject to a central point load $P$.
2. Use two beam elements to solve the problem of a beam of length $2 L$ fixed at both ends subject to a distributed load $p_{0} \mathrm{~N} / \mathrm{m}$, as shown in Figure 2.


Figure 2: A beam subject to a uniformly distributed load $p_{0}$.
3. Use two beam elements to solve the problem of a beam of length $2 L$ fixed at both ends subject to a linearly distributed load $p(x) \mathrm{N} / \mathrm{m}$, as shown in Figure 3.


Figure 3: A beam subject to a linearly distributed load $p(x)$.
4. A framework formed from two frame elements, shown in Figure 4, is subjected to a horizontal point force $P$. The extensional stiffness of the elements is $k=$ $E A / L$ and the bending stiffness is $\alpha=E I / L^{3}$. Formulate the matrices required to find the unknown displacements, forces and moments. Note: there is no need to solve the $3 \times 3$ matrices.


Figure 4: A framework formed from two frame elements

